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Investigation of momentum and kinetic energy correction coefficients in asymmetric compound cross-section flumes

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Abstract

A series of laboratory experiments was performed in order to investigate momentum and kinetic energy correction coefficients in asymmetric rectangular compound cross-section channels. The Reynolds number varied between 14,348.9 and 54,868.2, as relative depth (Y_r) changed from 0.155 to 0.825. Kinetic energy and momentum correction coefficients, α and β , were computed for 9 different models. As a result, the values of α and β considering 106 data points related to 9 distinct cross-sections averaged 1.1525 and 1.1261, respectively.

Key Words: Kinetic energy correction coefficient, momentum correction coefficient, open channels, compound cross-section, relative depth

1. Introduction

In open channel flow, normally the velocity distributions are not uniform over the cross-section; hence, the velocity head and the momentum flux are generally greater than the values computed by using the average velocity. These values may be corrected by using the so-called energy and momentum correction coefficients, which are always slightly greater than the limiting value of unity (Al-Khatib and Göğüş, 1999). Momentum and kinetic energy principles often are used in hydraulic problems ([Seckin et al., 2009](https://www.researchgate.net/publication/228362500_Experimental_investigation_of_kinetic_energy_and_momentum_correction_coefficients_in_open_channels?el=1_x_8&enrichId=rgreq-10780b9bf84cd8d6acab4251e90f0cc4-XXX&enrichSource=Y292ZXJQYWdlOzI2Nzk2MDg2MjtBUzoyNjA4NTE1NTA2NTAzNjhAMTQzOTIwMzI2NDA1OA==)). Momentum and kinetic energy correction coefficients, β and α , are often assumed to be unity when the momentum and energy principles are used in the computations as presented by many authors ([Chow, 1959;](https://www.researchgate.net/publication/259229312_Open-Channel_Hydraulics?el=1_x_8&enrichId=rgreq-10780b9bf84cd8d6acab4251e90f0cc4-XXX&enrichSource=Y292ZXJQYWdlOzI2Nzk2MDg2MjtBUzoyNjA4NTE1NTA2NTAzNjhAMTQzOTIwMzI2NDA1OA==) Streeter and Wylie, 1979; [French, 1987;](https://www.researchgate.net/publication/291506063_Open-channel_hydraulics?el=1_x_8&enrichId=rgreq-10780b9bf84cd8d6acab4251e90f0cc4-XXX&enrichSource=Y292ZXJQYWdlOzI2Nzk2MDg2MjtBUzoyNjA4NTE1NTA2NTAzNjhAMTQzOTIwMzI2NDA1OA==) Massey, 1989; [Chen, 1992;](https://www.researchgate.net/publication/245295264_Momentum_and_Energy_Coefficients_Based_on_Power-Law_Velocity_Profile?el=1_x_8&enrichId=rgreq-10780b9bf84cd8d6acab4251e90f0cc4-XXX&enrichSource=Y292ZXJQYWdlOzI2Nzk2MDg2MjtBUzoyNjA4NTE1NTA2NTAzNjhAMTQzOTIwMzI2NDA1OA==) [Roberson and Crowe, 1998;](https://www.researchgate.net/publication/41616232_Engineering_Fluid_Mechanics_CT_Crowe_et_al?el=1_x_8&enrichId=rgreq-10780b9bf84cd8d6acab4251e90f0cc4-XXX&enrichSource=Y292ZXJQYWdlOzI2Nzk2MDg2MjtBUzoyNjA4NTE1NTA2NTAzNjhAMTQzOTIwMzI2NDA1OA==) [Seckin et al., 2009](https://www.researchgate.net/publication/228362500_Experimental_investigation_of_kinetic_energy_and_momentum_correction_coefficients_in_open_channels?el=1_x_8&enrichId=rgreq-10780b9bf84cd8d6acab4251e90f0cc4-XXX&enrichSource=Y292ZXJQYWdlOzI2Nzk2MDg2MjtBUzoyNjA4NTE1NTA2NTAzNjhAMTQzOTIwMzI2NDA1OA==)). On the other hand, since it is not possible to have one-dimensional open channel flow, the true kinetic energy at a cross-section is not necessarily equal to the spatially averaged energy. To account for this, the kinetic energy and momentum correction factors are introduced, and the α and β generally are greater than unity.

Different theoretical expressions for α and β based on different assumptions and conditions have been derived by many authors ([Rouse, 1965;](https://www.researchgate.net/publication/284098764_Critical_analysis_of_open-channel_resistance?el=1_x_8&enrichId=rgreq-10780b9bf84cd8d6acab4251e90f0cc4-XXX&enrichSource=Y292ZXJQYWdlOzI2Nzk2MDg2MjtBUzoyNjA4NTE1NTA2NTAzNjhAMTQzOTIwMzI2NDA1OA==) Golubtsov, 1976; [Benedict, 1980;](https://www.researchgate.net/publication/246274939_Fundamentals_of_Pipe_Flow?el=1_x_8&enrichId=rgreq-10780b9bf84cd8d6acab4251e90f0cc4-XXX&enrichSource=Y292ZXJQYWdlOzI2Nzk2MDg2MjtBUzoyNjA4NTE1NTA2NTAzNjhAMTQzOTIwMzI2NDA1OA==) [Fox and McDonald, 1985;](https://www.researchgate.net/publication/265534176_Introduction_to_Fluid_Mechanics?el=1_x_8&enrichId=rgreq-10780b9bf84cd8d6acab4251e90f0cc4-XXX&enrichSource=Y292ZXJQYWdlOzI2Nzk2MDg2MjtBUzoyNjA4NTE1NTA2NTAzNjhAMTQzOTIwMzI2NDA1OA==) [Chen,](https://www.researchgate.net/publication/277663741_Unified_Theory_on_Power_Laws_for_Flow_Resistance?el=1_x_8&enrichId=rgreq-10780b9bf84cd8d6acab4251e90f0cc4-XXX&enrichSource=Y292ZXJQYWdlOzI2Nzk2MDg2MjtBUzoyNjA4NTE1NTA2NTAzNjhAMTQzOTIwMzI2NDA1OA==) [1991](https://www.researchgate.net/publication/277663741_Unified_Theory_on_Power_Laws_for_Flow_Resistance?el=1_x_8&enrichId=rgreq-10780b9bf84cd8d6acab4251e90f0cc4-XXX&enrichSource=Y292ZXJQYWdlOzI2Nzk2MDg2MjtBUzoyNjA4NTE1NTA2NTAzNjhAMTQzOTIwMzI2NDA1OA==)). Due to the limited data available in the literature especially for compound channels, β and α are often assumed to be unity in the computations for uniform flow.

2. Theoretical considerations

As mentioned previously, the velocity distribution is nonuniform in open channel flow. As a result, the velocity head of an open channel flow is generally greater than the value computed by using the average velocity. Therefore, the true velocity head may be expressed as $\propto \frac{U^2}{2g}$, where \propto is known as the kinetic energy correction coefficient, U is the cross-sectional mean velocity, and g is the gravitational acceleration. By definition, then the kinetic energy correction coefficient α is as defined in Eq. (1).

$$
\propto = \frac{1}{U^3 A} \int_A u^3 dA \tag{1}
$$

where u is the point velocity at each point in the cross-section, A is the flow area, and dA is the differential area in the whole flow area.

In the same way, in applying the momentum equation to open-channel flows with simple or compound cross-sections, the true momentum flux of an incompressible fluid passing a cross-section is given by the integral indicated by Eq. (2).

$$
\int_{A} \rho u^2 dA = \rho \beta U^2 A \tag{2}
$$

where ρ is the density of the fluid. The momentum correction coefficient, β , can be derived from Eq. (2) to yield the value presented in Eq. (3).

$$
\beta = \frac{1}{\rho U^2 A} \int_A \rho u^2 dA \tag{3}
$$

Typically, the values of \propto and β for various open channel cross-sections may be determined by either graphical integration or numerical methods using the measured velocity distributions as defined by Eqs. (1) and (3). Energy and momentum correction coefficients are often used in computer models for the determination of water surface profiles considering open channels with compound cross-sectional area, such as HEC-2 1991 and HEC-RAS 2002 ([Seckin et al., 2009](https://www.researchgate.net/publication/228362500_Experimental_investigation_of_kinetic_energy_and_momentum_correction_coefficients_in_open_channels?el=1_x_8&enrichId=rgreq-10780b9bf84cd8d6acab4251e90f0cc4-XXX&enrichSource=Y292ZXJQYWdlOzI2Nzk2MDg2MjtBUzoyNjA4NTE1NTA2NTAzNjhAMTQzOTIwMzI2NDA1OA==)).

In the present study, numerical integration was used for the calculation of the kinetic energy and momentum correction coefficients for asymmetrical rectangular compound cross-sections. The cross-sectional area (A) of the channel was divided into (N) number of elementary areas. For each elementary area (ΔA_i), the corresponding average velocity (u_i) was determined from the measured velocities. The cross-sectional average velocity (U) and the correction coefficients (\propto and β) were calculated using Eqs. (4) to (6).

$$
U = \frac{\sum_{i=1}^{N} u_i \Delta A_i}{A}
$$
 (4)

$$
\beta = \frac{\sum_{i=1}^{N} u_i^2 \Delta A_i}{U^2 A} \tag{5}
$$

$$
\propto = \frac{\sum_{i=1}^{N} u_i^3 \Delta A_i}{U^3 A} \tag{6}
$$

According to [Seckin et al. \(2009\)](https://www.researchgate.net/publication/228362500_Experimental_investigation_of_kinetic_energy_and_momentum_correction_coefficients_in_open_channels?el=1_x_8&enrichId=rgreq-10780b9bf84cd8d6acab4251e90f0cc4-XXX&enrichSource=Y292ZXJQYWdlOzI2Nzk2MDg2MjtBUzoyNjA4NTE1NTA2NTAzNjhAMTQzOTIwMzI2NDA1OA==), for the case where the velocities are unidirectional but nonuniform across the section, Jaeger in 1956 found that the kinetic energy correction coefficient (α) can be determined using Eq. (7) .

$$
\alpha - 1 = 3(\beta - 1) + \frac{1}{A} \int\limits_A \left[\frac{u - U}{U} \right] dA \tag{7}
$$

In order to investigate the variation in α and β in asymmetrical compound cross-sectional-shaped flumes, the present study was designed to obtain velocity distribution data. For this aim, a series of laboratory experiments were conducted in a compound channel flume. In addition, a general equation was derived to determine the relation between \propto and β using the entire data obtained from the 9 tested models.

3. Materials and methods

A series of laboratory experiments were done in an asymmetrical compound channel flume at the Fluid Mechanics Laboratory of Birzeit University, Palestine, to investigate the kinetic energy and momentum correction coefficients, \propto and β respectively. As can be seen from Figure 1, the flume consisted of a main channel and its asymmetrical floodplain.

 b) Cross section of the asymmetric rectangular compound channel Figure 1. Definition sketch of the flume used in the experiments.

The flume was glass-walled, 7.5 m long, 0.30 m wide, and 0.3 m deep, with a bottom slope of 0.0025. Discharge was measured volumetrically with a flow meter with 0.1-L accuracy. A point gauge was used along the centerline of the flume for head measurements. All depth measurements were done with respect to the bottom of the flume. A pitot tube of circular section with external diameter of 8 mm was used to measure the

static and total pressures, which were used to estimate the velocities and shear stresses at required points in the experiments conducted throughout this study.

Models of asymmetric rectangular compound cross-sections were fabricated from Plexiglas and placed at about the mid-length of the laboratory flume. Figure 1 shows the plan view and cross-section of the models with symbols designating important dimensions of model elements. Dimensions of various models used in the experiments are given in Table 1. In this study, the models tested are denoted by B_iZ_j (Bi = 10, 15, 20 cm; $Zj = 2, 4, 6$ cm). The B and Z dimensions represent the width and step height of the main channel of the asymmetric compound cross-section, respectively.

Model	В	Ζ	$\mathrm{B}_{\mathrm{\,\scriptscriptstyle{f}}}$	B_O	Θ_1	Θ_2	\rm{B}_{f} B_{O}	′Z B_O	B_O В	'Z $\mathrm{B}_{\mathrm{\it f}}$	$B_f/$ Έ	B/Z
	cm	cm ₁	$\,\mathrm{cm}$	$\,\mathrm{cm}$	(degrees)	(degrees)	$\overline{}$	$\overline{}$	-	$\overline{}$	$\overline{}$	$\overline{}$
$B_{10}Z_2$	10	2	20	30	26.57	153.43	1.50	15.00	3.00	10.00	2.00	5.00
$B_{10}Z_4$	10	4	20	30	26.57	153.43	1.50	7.50	3.00	5.00	2.00	2.50
$B_{10}Z_6$	10	6	20	30	26.57	153.43	1.50	5.00	3.00	3.33	2.00	1.67
$B_{15}Z_{2}$	15	$\overline{2}$	15	30	26.57	153.43	2.00	15.00	2.00	7.50	1.00	7.5
$B_{15}Z_4$	15	4	15	30	26.57	153.43	2.00	7.50	2.00	3.75	1.00	3.75
$B_{15}Z_6$	15	6	15	30	26.57	153.43	2.00	5.00	2.00	2.50	1.00	2.5
$B_{20}Z_2$	20	$\overline{2}$	10	30	26.57	153.43	3.00	15.00	$1.50\,$	5.00	0.50	10.00
$B_{20}Z_4$	20	4	$10\,$	30	26.57	153.43	3.00	7.50	1.50	2.50	0.50	5.00
$B_{20}Z_6$	20	6	10	30	26.57	153.43	3.00	5.00	$1.50\,$	1.67	0.50	3.33

Table 1. Geometrical properties of the asymmetric compound channel models.

The required experiments were first conducted in the models of smallest B $(=10 \text{ cm})$ with varying Z values ($=2 \text{ cm}$, 4 cm, and 6 cm) and then B was increased to 15 cm at the required amount of Z ($=2 \text{ cm}$, 4 cm, and 6 cm), and finally for B = 20 cm with the same 3 values of Z. The entrance angles, θ_1 and θ_2 , were 26.565 \degree and 153.35 \degree , respectively. The transition length was twice the floodplain width, B_f.

In order to obtain the velocity distribution in the 9 different asymmetric rectangular compound crosssections, the channel cross-section was divided into a number of vertical velocity profiles normal to the direction of flow. Then the total and static heads were measured at several points along these normal lines by the use of a pitot (Preston) tube. More points were taken close to the channel boundary. Towards the free surface, the distances between the points where the velocities measured were increased. Figure 2 shows a definition sketch for vertical lines over which velocity measurements were made in models B_iZ_j (Bi = 10, 15, 20 cm; Zj = 2, 4, 6 cm).

4. Results and discussion

For different relative depth values, the computed values of the kinetic energy and momentum correction coefficients of the 9 models are given in Table 2. They are related to the relative depth (Y_r) because it reflects the geometry effect on the discharge distribution in compound cross-section channels as Y_r is defined as the floodplain depth to the total depth associated with the compound cross-section(Y_f/h) which is a dimensionless quantity.

Figure 2. Definition sketch for vertical lines over which velocity measurements were made for the different models (dimensions are in cm).

There is a large difference in the velocity distribution between main channel and floodplains for compound channels. That is why for the 9 asymmetrical compound channels tested in this study, the values of α and β averaged 1.1525 and 1.1261, respectively, while they averaged 1.0604 and 1.0222, respectively, for single channels (Blalock and Sturm, 1981, 1983). This means that the average values of α and β for channels with simple cross-sections are lower than their corresponding values associated with compound channels. In a study conducted by Seckin et al. (2009) considering a symmetrical compound channel, it was determined that the average values of the kinetic energy and momentum correction coefficients α and β were 1.1309 and 1.0458, respectively. This also means the (α and β) average values for symmetric rectangular channels are lower than their corresponding values for asymmetric compound channels.

As it can be noted from Eq. (7), the last term is often small because the integral always changes sign (Seckin et al., 2009). Thus, it makes sense to seek a linear regression between $(\alpha -1)$ and $(\beta -1)$. For the 9 different asymmetric compound channels, the values of $(\infty -1)$ versus the values of $(\beta - 1)$ are plotted in Figure 3, which shows a strong linear correlation between the 2 plotted values. Therefore, a simple linear single-variable regression model is formulated using all 106 data points derived from the 9 tested asymmetric

Table 2. Continued Table 2. Continued

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cross-sections. The generated model is presented in Eq. (8), which can be used to predict the ($\propto -1$) value as a function of $(\beta - 1)$ value for an asymmetrical rectangular compound cross-section. This regression model is associated with a very high correlation coefficient value $(R$ -squared $= 0.998$).

$$
(\alpha - 1) = 0.990(\beta - 1) + 0.027
$$
\n(8)

In addition to the relationship between ($\propto -1$) and ($\beta - 1$), the relationship between α and β is also shown in Figure 4 using all 106 data points generated from the 9 cross-sections with the corresponding regression model given by Eq. (9) .

$$
\alpha = 0.990\beta + 0.037\tag{9}
$$

Normally, the velocity distribution in the flumes is determined by the shape and roughness of the channel. All data presented in this study are limited to flumes with smooth surfaces and the possible effects of the surface roughness were not examined. Thus, the averaged values of \propto and β proposed herein are recommended for asymmetric compound smooth surface open channels.

Figure 3. Relation between $(\alpha - 1)$ and $(\beta - 1)$. **Figure 4.** Relation between kinetic energy correction factor (α) and momentum correction factor (β) .

Values of the Reynolds number (Re) for the different tested models are estimated using Eq. (10) and are presented in Table 3.

$$
Re = UD/\nu \tag{10}
$$

where D is the hydraulic depth, which is defined as the cross-sectional area of the water normal to the direction of flow in the channel divided by the width of the free surface; ν is the kinetic viscosity of water. As can be seen from Table 3, Re varied between 14,348.9 and 54,868.2, as relative depth (Y_r) changed from 0.155 to 0.825.

It can be clearly seen from Table 3 that as the discharge decreases $(Y_r$ values decrease) the values of Re decrease, which is true for all tested models.

Model										
$B_{10}Z_2$		$B_{10}Z_4$			$B_{10}Z_6$	$B_{15}Z_{2}$		$B_{15}Z_4$		
Y_r	Re	${\rm Y}_r$	Re	Y_r	Re	${\rm Y}_r$	Re	Y_r	Re	
0.818	50,694.1	0.669	44,620.4	0.559	45,608.7	0.825	53,326.0	0.640	47,576.8	
0.815	49,302.6	0.664	42,975.4	0.542	42,991.3	0.817	50,527.9	0.633	45,713.1	
0.810	47,414.4	0.655	42,235.1	0.524	40,965.1	0.811	49,117.3	0.615	40,959.5	
0.802	44,741.0	0.646	40,500.9	0.504	37,839.5	0.789	43,402.8	0.630	45,145.3	
0.792	41,329.5	0.633	39,356.7	0.483	33,786.8	0.785	41,033.0	0.612	39,762.2	
0.780	36,889.5	0.619	36,413.8	0.464	30,928.3	0.770	36,931.6	0.600	37,615.2	
0.765	33,464.7	0.596	32,423.7	0.444	28,206.9	0.756	33,975.2	0.579	34,377.2	
0.744	29,700.9	0.565	28,465.3	0.429	26,264.3	0.744	32,153.4	0.551	31,420.1	
0.733	27,690.5	0.545	27,001.0	0.394	23,859.4	0.722	28,755.9	0.524	28,694.9	
0.701	24,671.4	0.512	23,878.2	0.368	21,728.9	0.697	25,241.0	0.494	25,915.7	
0.661	19,249.2	0.459	19,380.8	0.310	17,962.8	0.672	22,304.1	0.459	22,744.4	
0.592	14,348.9	0.394	14,835.3	0.268	15,067.2	0.636	19,982.9	0.385	18,300.9	

Table 3. Reynolds number for various types of models.

Table 3. Continued.

Model										
	$B_{15}Z_6$		$B_{20}Z_2$		$B_{20}Z_4$	$B_{20}Z_6$				
Y_r	Re	Y_r	Re	Y_r	Re	Y_r	Re			
0.504	46,749.0	0.821	54,868.2	0.649	$\overline{51,290.7}$	$\overline{0.5}12$	50,827.1			
0.496	45,120.5	0.802	50,258.7	0.630	47,898.9	0.500	$\overline{48,922.9}$			
0.478	42,997.7	0.789	47,109.4	0.626	$\overline{46}, 122.9$	0.469	46,011.7			
0.455	38,846.9	0.787	45,448.3	0.615	44,258.9	0.417	40,639.9			
0.444	37,111.8	0.785	43,779.5	0.592	40,719.9	0.400	38,396.8			
0.423	34,158.0	0.780	42,657.6	0.565	37,479.0	0.388	36,848.1			
0.400	31,510.3	0.756	36,540.0	0.545	35,663.3	0.362	33,758.6			
0.375	29,551.6	0.733	33,748.3	0.518	32.694.1	0.294	29,206.8			
0.326	26,721.8	0.718	30,712.2	0.481	29,507.3	0.250	26,309.0			
0.259	22,171.4	0.706	27,590.9	0.452	27,263.4	0.189	23,170.2			
0.231	19,724.1	0.655	22,185.8	0.322	20,339.8					
0.155	16,210.9	0.574	16,843.7	0.286	18,454.9					

The value ranges associated with α and β as presented in this study (Table 2) can be utilized for practical purposes considering the geometric conditions (Table 1) under which velocity measurements were conducted in asymmetrical rectangular compound cross-sections and the same range of Re. The estimated α and β value ranges can be used for models of the same geometry and the same range of Re in order to calculate the energy and momentum flux of the flow for a particular cross-section.

5. Conclusions

In the present study, a series of laboratory experiments was conducted to investigate the momentum and kinetic energy coefficients in channels with asymmetric rectangular compound cross-sections. Two linear single-variable regression models for estimating (\propto -1) as a function of (β -1) and \propto as a function of β were formulated using all 106 data points obtained from the 9 tested cross-sections. This study explored the practical average

values of α and β and found them to be 1.1525 and 1.1261, respectively, considering the 9 different straight asymmetrical compound channel flumes. The range of kinetic energy coefficient and momentum correction coefficient values can be used for practical purposes for models of the same geometry and the same range of Re.

Nomenclature

- A whole flow area
- B bottom width of the approach channel
- B_f floodplain channel width
- B_O bottom width of the upstream channel
- D hydraulic depth
- dA an elementary area in the whole flow area
- g gravitational acceleration
- h main channel water depth
- N number of small areas, ΔAi
- Q average full cross-sectional discharge
- u point velocity at each point in the cross-section
- U cross-sectional mean velocity
- r correlation coefficient
- Y_f floodplain water depth
- Y_{mc} h, main channel water depth
- Y_r relative depth, which equals the Y_f/Y_{mc} ratio Z step height
	-
- α kinetic energy correction coefficient β
- momentum correction coefficient
- ν kinetic viscosity of water
- θ_1, θ_2 entrance angles
- ρ density of the fluid

References

Al-Khatib, I.A., and Göğüş, M., "Momentum and Kinetic Energy Coefficients in Symmetrical Rectangular Compound Cross Section Flumes", Turkish Journal of Engineering and Environmental Science, 23, 187–197, 1999.

[Benedict, R.P., Fundamentals of Pipe Flow, John Wiley and Sons, New York, N.Y., 1980.](https://www.researchgate.net/publication/246274939_Fundamentals_of_Pipe_Flow?el=1_x_8&enrichId=rgreq-10780b9bf84cd8d6acab4251e90f0cc4-XXX&enrichSource=Y292ZXJQYWdlOzI2Nzk2MDg2MjtBUzoyNjA4NTE1NTA2NTAzNjhAMTQzOTIwMzI2NDA1OA==)

Blalock, M.A., and Sturm, T.W., "Minimum Specific Energy in Compound Open Channel", ASCE Journal of the Hydraulics Division, 107, 699–717, 1981.

[Blalock, M.A., and Sturm, T.W., "Closure for Minimum Specific Energy in Compound Open Channel", ASCE Journal](https://www.researchgate.net/publication/288672604_Minimum_specific_gravity_energy_in_compound_open_channel?el=1_x_8&enrichId=rgreq-10780b9bf84cd8d6acab4251e90f0cc4-XXX&enrichSource=Y292ZXJQYWdlOzI2Nzk2MDg2MjtBUzoyNjA4NTE1NTA2NTAzNjhAMTQzOTIwMzI2NDA1OA==) [of the Hydraulics Division, 109, 483–486, 1983.](https://www.researchgate.net/publication/288672604_Minimum_specific_gravity_energy_in_compound_open_channel?el=1_x_8&enrichId=rgreq-10780b9bf84cd8d6acab4251e90f0cc4-XXX&enrichSource=Y292ZXJQYWdlOzI2Nzk2MDg2MjtBUzoyNjA4NTE1NTA2NTAzNjhAMTQzOTIwMzI2NDA1OA==)

[Chen, C.L., "Unified Theory on Power Laws for Flow Resistance", J. Hydr. Engrg., ASCE, 117, 371–389, 1991.](https://www.researchgate.net/publication/277663741_Unified_Theory_on_Power_Laws_for_Flow_Resistance?el=1_x_8&enrichId=rgreq-10780b9bf84cd8d6acab4251e90f0cc4-XXX&enrichSource=Y292ZXJQYWdlOzI2Nzk2MDg2MjtBUzoyNjA4NTE1NTA2NTAzNjhAMTQzOTIwMzI2NDA1OA==)

[Chen, C.L., "Momentum and Energy Coefficients Based on Power-Law Velocity Profile", J. Hydr. Engrg., ASCE, 118,](https://www.researchgate.net/publication/245295264_Momentum_and_Energy_Coefficients_Based_on_Power-Law_Velocity_Profile?el=1_x_8&enrichId=rgreq-10780b9bf84cd8d6acab4251e90f0cc4-XXX&enrichSource=Y292ZXJQYWdlOzI2Nzk2MDg2MjtBUzoyNjA4NTE1NTA2NTAzNjhAMTQzOTIwMzI2NDA1OA==) [1571–1584, 1992.](https://www.researchgate.net/publication/245295264_Momentum_and_Energy_Coefficients_Based_on_Power-Law_Velocity_Profile?el=1_x_8&enrichId=rgreq-10780b9bf84cd8d6acab4251e90f0cc4-XXX&enrichSource=Y292ZXJQYWdlOzI2Nzk2MDg2MjtBUzoyNjA4NTE1NTA2NTAzNjhAMTQzOTIwMzI2NDA1OA==)

[Chow, V.T., Open-Channel Hydraulics, McGraw-Hill, New York,](https://www.researchgate.net/publication/259229312_Open-Channel_Hydraulics?el=1_x_8&enrichId=rgreq-10780b9bf84cd8d6acab4251e90f0cc4-XXX&enrichSource=Y292ZXJQYWdlOzI2Nzk2MDg2MjtBUzoyNjA4NTE1NTA2NTAzNjhAMTQzOTIwMzI2NDA1OA==) 1959.

[Fox, R.W., and McDonald, A.T., Introduction to Fluid Mechanics, John Wiley and Sons, New York, N.Y., 1985.](https://www.researchgate.net/publication/265534176_Introduction_to_Fluid_Mechanics?el=1_x_8&enrichId=rgreq-10780b9bf84cd8d6acab4251e90f0cc4-XXX&enrichSource=Y292ZXJQYWdlOzI2Nzk2MDg2MjtBUzoyNjA4NTE1NTA2NTAzNjhAMTQzOTIwMzI2NDA1OA==)

[French, R.H., Open-Channel Hydraulics, McGraw-Hill, Singapore. 2nd edition,](https://www.researchgate.net/publication/291506063_Open-channel_hydraulics?el=1_x_8&enrichId=rgreq-10780b9bf84cd8d6acab4251e90f0cc4-XXX&enrichSource=Y292ZXJQYWdlOzI2Nzk2MDg2MjtBUzoyNjA4NTE1NTA2NTAzNjhAMTQzOTIwMzI2NDA1OA==) 1987.

Golubtsov, V.V., "Dependence of the Coriolis and Boussinesq Coefficients on the Slope of a Mountain Stream", Soviet Hydrology: Selected Papers, 15, 41–43, 1976.

Massey, B.S., Mechanics of Fluids, Chapman and Hall Ltd., London. 6th edition, 1989.

[Roberson, J.A., and Crowe, C.T., Engineering Fluid Mechanics, John Wiley & Sons, Inc., Canada. 6th edition, 1998.](https://www.researchgate.net/publication/41616232_Engineering_Fluid_Mechanics_CT_Crowe_et_al?el=1_x_8&enrichId=rgreq-10780b9bf84cd8d6acab4251e90f0cc4-XXX&enrichSource=Y292ZXJQYWdlOzI2Nzk2MDg2MjtBUzoyNjA4NTE1NTA2NTAzNjhAMTQzOTIwMzI2NDA1OA==)

[Rouse, H., "Critical Analysis of Open-Channel Resistance", J. Hydr. Div., ASCE, 91\(h4\), 1–25, 1965.](https://www.researchgate.net/publication/284098764_Critical_analysis_of_open-channel_resistance?el=1_x_8&enrichId=rgreq-10780b9bf84cd8d6acab4251e90f0cc4-XXX&enrichSource=Y292ZXJQYWdlOzI2Nzk2MDg2MjtBUzoyNjA4NTE1NTA2NTAzNjhAMTQzOTIwMzI2NDA1OA==)

[Seckin, G., Ardiclioglu, M., Cagatay, H., Cobaner, M., and Recep Yurtal, R., "Experimental Investigation of Kinetic](https://www.researchgate.net/publication/228362500_Experimental_investigation_of_kinetic_energy_and_momentum_correction_coefficients_in_open_channels?el=1_x_8&enrichId=rgreq-10780b9bf84cd8d6acab4251e90f0cc4-XXX&enrichSource=Y292ZXJQYWdlOzI2Nzk2MDg2MjtBUzoyNjA4NTE1NTA2NTAzNjhAMTQzOTIwMzI2NDA1OA==) [Energy and Momentum Correction Coefficients in Open Channels", Scientific Research and Essay, 4, 473–478, 2009.](https://www.researchgate.net/publication/228362500_Experimental_investigation_of_kinetic_energy_and_momentum_correction_coefficients_in_open_channels?el=1_x_8&enrichId=rgreq-10780b9bf84cd8d6acab4251e90f0cc4-XXX&enrichSource=Y292ZXJQYWdlOzI2Nzk2MDg2MjtBUzoyNjA4NTE1NTA2NTAzNjhAMTQzOTIwMzI2NDA1OA==)

Streeter, V.L., and Wylie, E.B., Fluid Mechanics, McGraw-Hill, New York, 1979.